

0031-3203(W)E0019-11

13.41-WEIGHTED SKELETON DECOMPOSITION FOR PATTERN REPRESENTATION AND DESCRIPTION

Hinnes di Cidennetal, UNE, Via Teanu & NUT? Ann Behal. Naples, tala Equipe TIMC-IMAQ, CERMO BP 51, Shull Littinshib Celux 9, France GABRILLA SANNITI OF BARAT UPS EINETRIN THERE,

(Keeping & if of 1991, econical for publication 14 befores) 1994

pattera are anciditares, unide tenetificial quine, teoristeriolida do The excelling alculain comporent are haid do represent and dea ons strough the ulcompession of its (1/4) weighted states; space, where the three countinues of any fine patena is decomposal. Decomposition at Gifferen resolution. Energical values during the polyposal approximation, perfor purce, and the successive relenging the

Label of skeleton Polygonal approximation Decomposition Weight ad distance

each decomposition component could be interpreted as the representation of une of the regions constituting the pattern " Then, the description of the pattern is lion of each elementary region, which by hypothesis is characterised by a simple shape, can be obtained by tation of the pattern is decomposed, in such a way that obsisted in terms of the description of the obtained exploiting the information carried on by the contexpondisted by the structural approach. A suitable represenregions and of their spatial relationalism. The descripcomponent of the representation system.

The labelled skeletonia-111 is a convenient soci to the cibbon-like regions constituting the pattern. The analyse the shape of patterns perceived as union of tibbon-like tegions. A ribbon-like pattern is characterised by one spine and a disc. the disc sweeps out the moving along the sprine, thanging size as it moves. The skeleton is a curvilintar subset of the puttern and its branches play the role of the spines of Layed of any pixel p of the skeleton, which represents the distance of p from the complement of the patiena. can be interpreted as the radius of the sweeping disc centied on p. The shape of the disc depends on the if a quasi Euclidean metric is adopted shape by

tance are provided by the weighted distance furb-tions. 144-179 where thinkbelanger weights are used to

measure the distance between neighbouring pixels, depending on their relative position. Skelenas^{1,10,13,11} the steleton jabelted according to the city block or the cheschoerd distance can be obtained at a comparable (timited) computational cost. The stability of the weighted skeletons under pattern rossilan (avours their use for practical applications.

A concespendence exists between any subset of the Weleton and the region of the pallern that is the of the dux's associated with the pirels of the at eleton subsettin the strict sense, the only pixels of the stekton to recover the region). This region can be ablained by the skeleton subsel, which requires two caster scan contain circumstances, a saidactory approximited purational cost For instance, if the steleton subset can he interpreted as the spine of an elementary region having linearly (and monotonically) changing width and critatalion, a satisfactory approximated region is the ensetape of only two dists, those associated with sersion of the region can be oblizined at a lower com subset which are centres of maximal dists are enough applying the teverse distance transformation^{(48,196})

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art firration and for each periodent at elektron histori, the protection whose referance is evaluated is the protection raspect in the union of the cuttern periodical technology technology branch with the magh bouring at electron. skekton branchen froming is irerated until beanch removaldoes not elmimish the representative power of neighbouring branches literating pruding does ook eaute assummation effect to the loss of information. At by branch points may be prunted as 1000 as they become peripheral branches, due to the ekknon of the

bracket, already present at a particula translag. To the particular, the followation relative to the translag of point (a) of the beautiful it propagated through the brackfest while performing parating. In fact, a the [Adjuscational statement as present of the [Adjuscational statement as present of the fact of the point of the propagated statement of the propagated of the propagated of the particular of t does not judicide all the maximal centers of B. In Fig. 19th, the amonoting effect due to the present pro- decret is effectly tack at the control permatance after report. The strategies is preferring the documposed into the control permatance for includes. This is equivalent to perform a decomposing the tenter into the performing a decomposition of the parties to performing a decomposition of the parties to performing a decomposition of the parties to the performing a decomposition of the parties to the performance of the parties of the par

the entremes of the Stekens bisinches and the spatial spolyleg the treers distance transformation to the Each skilteen branch is furthermore decomposed, by means of a polygonal appopulation, in such a way that each perilinear negment constitutes the 19the of an elements y region. Division points have to be placed wherever non-linear currenties changes occur along changes along the contour of the corresponding pattern tubiet... Dirition points have also to be placed where relationships among them

non-linear or non-monotonic label variations occur. as they indicate host-facar or non-monotonic pattern Inkeness variations. To locate both lypes of division points, we interpret any skileton beanch as an are in tabel. Using the normalized tabelin place of the distance label is done to tress redoctaly the three coordinates. by allowing a displacement of one wait only in each of the three directions, when parxing from a steletal pitel to one of its neighbours. In this way the skeletost 3D apace where for each skeletal pitel, the three coordinated are the planning coordinates and the normalised

using a tylitype algorithm (t.g. the one described by Particis, the collained set of vertices is not unfluenced by the order in which stelessing piech are processed. The extremes of the cuttent branch (say of The polygonsh approximation is accomplished by

The Guilden Chirace 4/(p) between uny fried p 1st the teletop branch and the ID strüght line (ep.eg) is that d_e(g) is greater than an a priori first threshold B. Vertes telection is then accomplished on the sub-ares computed. Then, the pixel of the bisach for which defer ago and ever. The recorreive process terminates when, for has the largest value in tallon as a new nutter r, provided (and stored in the data titucture) in a recutifive way

If a number of pirels of the akthem branch man mites delph the two prieds which me respectively the neurively exemised Accepting severites all the pines ma timized delta could result in a polygonal approxienation with too many vertices, not necessarily all closest to s, and to e, are accepted as vertices, and the ignificant, In contrast, accepting only one pivel could make the ateleton documposition dependent on the eketerion are is divided in three sub-area, which are the pixel maximizing defat, it results in defat 5 d. order in which the pricity are propested.

The square root compulation accessary to obtain the Evelocan distinct Lighten be avoided, since the state road in obtained in hen computing the square distance with the square distance with the square distance with the square distance.

tougher and rougher, in fact, the regions that could be recovered by applying the revelse distance transformation to applying the chestral component are labely to differ tenantiably from the correlation of the confidence of the regarded as acceptable for the specific test. The three-hold about the surfer most, in farour a quite faithful ecouping of the elementary regions harring the sheleton regimen, by building the earthopes of The value of 0 is timed depending on the toberings The pain of discs, contribe on the statement of the appirer. In our superioration, the value $\theta=1.5$ has been resident substants. Statement ordinary positions at different resolution levels is obtained by assigning different values to fl. As the threshold foctears, the number of comrally diminishen, while the representation becomes process into which the steleton is decomposed gene-

P(0) Any subset is obtained by comparing the value delpt, using Kor any piret p of P(0), with the desired approximation of the iteleton, performed with the can be directly ideatified at they conjutute a tybest of Lat V(P) to the set of vertices found in the polygonal owen threshold. The vertices of hay other polygonal specialization, performed with a district threshold new threshold.

approximations of the skewton at Recortery of the elementary regions represented by the theiston segments is not necessary for computing here features east early to derived statting from the prometrie features (e.g. area or perimeter) and shape esteres (4.g orientation of rectargularity) of the regions 3D exercinates of the found vertices. However, first three different threshold values, are shown in Fig. 4. ing to polygonal

found during the polygonal approximation of the stateon with into elementary regions, fortesponding to $\theta=1.5\,(h)$ $\theta=4$ (c), and $\theta=5\,(\phi)$ (3,4) Weighted skeleton decemposition Fig. 4. Letter V decisions the vertices found during 1 Directed 8 - 1.3 (at decopyposition into chineniary Ţ

To use all the pattern representations is a compact way, we associate each wreat a of V(b) a quadruplet (s.y. label, d.(c)). In this way, the permanence of a wreat in any of the resolution levels can be immediately

chacked. In Table 1, the entries x, y, i, e and e indicate the Carristian coordinates a say y, the table, the 3D distance, and the pixel type, respectively (b, e, and n, stand for branch point, end point and morntal point.

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contaithaithn l'. l'..... 7, 13 contidered, and

inns shown in Fig. 4. Ite regions are not elementary Polygonal approximation of the skeleton, performed with 0 = 1 5. Were that, in contrast to the demaposit-

The possibility of merging thems thating a branch point as a common vertex could also be taken into account, so that the final pattern dreen position would of the skeleton into its considering for makes. Work in not be conditioned by the predictinary decom this respect is custonly in progress.

patterns that can be perceived as constituted by the union of clanguated (tibbon like) regions, it would be In this paper we have illustrated a mathod for de Composing a digital pattern through the decomposition of its weighted skekton. The method is adequate far employed, for instance, in the framework of a document analysis task to classify the alphanumeric symbols which it contains

The weighted (Adaton has been chosen to favorie the stability of the decomposition under pattern retation. In fact, stability is an indispensable presupposition for

> have been used for the merging threshold t. The hree decompositions are obtained starting from the

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with reference to the straight line segment joining v. and z. The proves is repeated until for the concentraion $v_{k+1+\cdots k}$, $\{k=1+k, j=n-k, i>0\}$ the merging condition is scrifted by all the services. Then, czeh of these vertica the merging tatio 0,71, is cheeked

the merging condition is recursively checked on the two sub-concatenations tippi---- fig. and py. maintain thair region representation power, slace the region associated with a complex spine is the union of regions associated with the merged ite spines are taken as the extremes of the resulting The vertices definiting the set of the merged success. complex spine. Note that the remaining vertices still The value of the merging threshold a depends on the In our experiments, the value 1 = 0.25 has been adopted as a default value. Larger values can be used to favour merging. An example is shown in Fig. 7, where three different values desited merging, tolerance. the cementary Spines.

Fig. 8. Stability of the docomposition under pattern rotation

Fig. 7. Different decemposenens of the many partern, obtained by using defences rathers for the memping stackbold: 1 - Different december 1 - Diff fals 1 - O 20(ct. ã G. Saxann by Bara and E. Tiett

correspondence of which it is F = 1. Morcover, let vo [et ('e)....t belonging to the same steleton branch, is examined Let (r. . . . r.) and (v. e. . .) \mathcal{L} be the Exclidean distance of v_i from the straight line Each pair of recessive spines,

joining or with a ... is divided by the leagth L, of the segment for every or (im 1,2,..., n) If D,/L, < x for If a = I, the two spines (rous) and it was I are If n > 1, the distance D, from the straight line segment meered by all means Q is set to I in correspondence with each yerrer r, tuch segment joining e, ..., and e, ..., and the Euclidean length of the segment, respectively. A flag F, initially equal to that Diff., is less than an a priori fixed merging thre-

PAGE 5/34 * RCVD AT 4/14/2005 5:30:30 PM [Eastern Daylight Time] * SVR:USPTO-EFXRF-1/0 * DNIS:8729306 * CSID:312 580 9696 * DURATION (mm-ss):13-56

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The Interpretation and Reconstruction of Interfering Strokes

Document Processing Group, Center for Automatica Research University of Maryland, College Park, MD 20742-3111 David S. Doermans and Atriel Rosenfeld

uing perrepual katoru of the demus to texmitreet literrecting regious. By treating the strokus as leaturn and retaining a more detaind representation of the document, we can use criteria and dues for interpretation which are not available from traditional This paper addresses the problem of the interpretation of interfering conterns by approaches to document processing.

I Introduction

be detected, it would then be useful to recover the stroken and markings which participate in the interference, so that subsequent analysis and recognition algorithms will have the benefit of a more complete representation or charge features. One promiting approach to interpretake such interactions is to use properties of the affected stroken or multings as well as other In many document understanding domains, complications arise when handwritten strokes interact with themselves or with other markings on the document. If such interferences can keawledge about the domain to reparate the interfering features.

In our research we address the problem of the interpretating and reconstructing band-written stockes and machine-produced the regments whose structure has been affected by interaction either with each other or with other document features. Handwritten strukes may cross, merge, or otherwise touch; our god is to recover the instrument trajectory which gave tise to the features and the properties of the corrupted regments.

The extrapolation of a thin-line stroke representation into ongular regions (i.e., junctions) have on extremt has been addressed by Nisheka and Marie ([9]). One work in based on an intensity interceptual stroke and extends the analysis to general stroke/feature interceptual. Reconstruction has also been addressed by Wang and Srikati, who describe interceptual. Reconstruction has also been addressed by Wang and Srikati, who describe in approach to character splicing based on cut points between a line and a character ((4)).

2 Approach

Our approach to the problem of interfering contours is based on the detection, analysis and detailed representations of the stroke-like and non-stroke-like regions in the document intege. The process involves two parture as interpretation of the intersecting region and a recentivation of the aboves of like segments which formed it.

An interpretation of a region is derived from the boal configuration of a troke regionals.

analysis relies on the concept of a strake recovery platform to provide a comprehensive and adaptable representation of the document and is described briefly in Section 3. In Section and from properties of the strokes themselves such as currature, width and intentity. Our we discuss the example of a bacdwritten etroke intersecting a single isolated line segmeet. In Section 5 we provide a chasification of general stroke interactions (e.g. merges,

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contings, abutrectit, e.c.). We also provide a method of interpretating and whimalely recon-structing the intersection region wing the existence of uncorrupted boundaries, smoothness constraints, and properties of the incorning stroke segments.

3 The Stroke Recovery Platform

the concept of a stroke recovery platform, which is cucnibed in [1, 2]. The platform provides a biererchied representation of the stroke-lise features in a document, extending from the The framework used to address the interpretation and reconstruction problems is based on

platform contains, most importantly, a set of cross-section groupings which exhibit streke like properties (hypothesized stroke segments), region which we classified at possible junctions or endpoints, and the underlying tonious or contour fragments of the stroke segments, junctions, endpoints and understified features in the image. The stroke graph repports tog-down access to the pixels through the junctions, strokes, cross-sections and stinodopic Figure 1 thows a subset of the features computed for each region of the image. pixel level up through an attributed attoke graph. (pixel-tevel) information.

4 Stroke/Line Segment Interaction

the areas which result from a superposition of presumably independent markings and to delineate the original contours of the stroke and the line. segment. This example is sufficient to illustrate the time problems and serves as a basis for banding recovery tasks involving more complex interactions. Our grass are to isolate To illustrate how the stroke platform can be used to address feature interaction problems we consider the intersection of a kandwritten stoke with a straight, machine produced line

bounded by two apparent journions and has erees sections of significantly greater width than the corresponding lets or sight end segments. Since such changes contradict the usuruption of consistency, such a situation about he examined for possible leterpretation as resulting After we have constructed the stoke platform (Figure 1) we identify those portions of the correspond to interacting features. If properties of the line segment features such as width, position and orientation are known a priori, the stroke graph can be examined and the features identified. More realistically, we may identify line segments hand on the regularity and tire of the cross-sections comprising the hypothenized titoke expression. In eilber case, if the expansi interacts avolber seature, we will find a node in the stroke graph corresponding to the inserection. If the interaction occurs over an extended region, the affected portions of the titoke graph will have cross-section widths which are incombitent with the rest of the line segment. In Figure 1b, for example, the top-center strake tegrates is

(Figure 2). Since the line regment is of known dimenisms, we generate (or retrieve sa part of our a priori knowledge) a cross section representation of the model line regiment and register As stated extiter, the recenstraction is based on properties of the pontions of the document that do not invoke feature interactions. We first identify eacher points which are used to connect the reconstructed feature segments to known feature regments. We identify a set candidate anchor point pairs from the exonesections at the eads of the effected segments is with the representative given by the platform. Figure 3 thous a set of ideal cross sections Once we have an approximate delineation of the line segment, we begin the reconstruction. from an interaction of features.

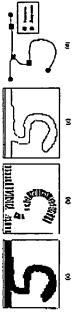


Figure 1: Several components of the platform which result from the processing of the donement region (4).

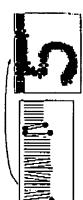


Figure 2: The candidate anchor points derived from the cross section endpoints.

overlayed on the image. From this correspondence, we can easily identify the isolated lies regress features which are uncourapted and reface the registration if necessary. We then clessify contours between the anchor points of the hypothesised stroke segments which do do not fit the model.

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by naise in the intensity image. A contour is unstable if its foration or orientation may be Bounded partions of the contours are described as follows. A wisible contour is a boundary regruestation of a stroke or region that is derivable from areas of high gradient activity in the image. An occluded contour is a boundary of a stroke or line segment which is observed os otherwise distorted by another strake or live segment. A montour is suid to be stakke if it excresponds to an occorrayied postion of the stroke and is itself free from distortion crused corrupted by acideboring strokes.

is connected to the comming part of the stroke segment, so we can assume that it is part of the same stroke. We use the properties of the unocoluded stroke segments to reconstruct the contour and delineate the region which corresponds to the occluded stroke (Figure 35). condination tross sections, contours and atrake graph components. If necessary the orchoded The occluded stroke segment contour is then reconstructed from the remulaing visible The pittions can thus be annotated to reflect line-regiment, non-time-segment and possible line segment contour is existy recovered from the model by generating its location and pasicontours and eachor points. For the intersection in this example, the visible strake contour tion from the visible trable contour.

5 General Stroke/Stroke Interaction

goalthers. Without has of generality, it is sufficient to discuss only the interaction among section we describe in more detail the stroke extragalation and seconstructive at-12 1552

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(a) {b} Figure 3: The reconstructed line segment in registration with the original image and the stroke recovered from the uncorrupted boundary

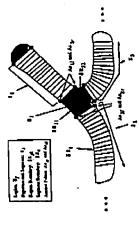


Figure 4: Landmark features for stroke reconstruction

hand-produced stroke segments; their interaction with mathine-produced segments is simply a special case where the regularity of the line segment features reduce the complexity of the processing and the number of possible interpretations. Figure 4 shows some of the platform components including errors actions, arrives points and stroke and regions bornedaried.

component interacts the executes, are present an extension of the set of associated. Our goal is to interpret each near-time region as an extension of the set of associated exgrants (extrayolation) and to recover the occal-code stroke contains and cross sections (reconstruction). In general, the validity of an intersection region interpretation will be based on 1) the general the regions painings, 2) the competibility of the stroke reconstructions with the region in question, and 3) genetally imposed by higher level understanding of the writing.

5.1 Smoothness

Smoothness is a local mensure of the confidence that a given pair of segments itad jure Smoothness, portions of the same stocke, extending through a region k. In general, we define smoothness, E. for each pair of segments itad juavering a non-stocke region k as



Figure 5: Smoothtess parameters

$$P(i,j,k) = P(\vec{a},\vec{k},\vec{k},\vec{k},\vec{k},\vec{k}) \quad \vec{P} = \{p_1,p_1,...,p_n\}$$

$$= \bigoplus_{n=1}^{\infty} \sum_{i=1}^{n} f_i(p_{in},p_{jin},p_{jin})$$

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where \vec{p}_i , \vec{p}_j , and \vec{p}_d are property vectors computed from the conservating segment and region features, the f_{ij} are emorchment functions of individual features properties and \vec{o} is a weight vector. The $\vec{0}$ operator is a foundary non-inear) combination of the smoothness consultation is based on perceptual organisation criteria involving the position, correttee and feature consistency of the associated arguments appear from boundary features within the non-stroke region.

First we define the computation of a set of local properties within each region. At each stroke anchor point, 4, we estimate the angle of the boundary measured from the borizonal axis, os, and the righ of its curvalent, s., and make its orientation. In addition, for each axis, os, and the righ of its computative, s., and make its orientation. In addition, for each taking of pacific points, we compute the sagin, 7, of a line segment connecting them in the direction of positive orientation (Figure 3). From these parameters, we are proportied as he computed including:

Given an anches point pair, we wish to define O set that it is maximal in the succeibtest case. If we assume that a streke thould form a ribbon-like region, the properties derived frican the two sets of anches point pairing can be averaged to give property ruless for the stroke. Similarly, the properties which are computed for more than two anchor points along the stacks extricts can be averaged to produce a single value.

Departing on the configuration of the incoming area, different annothness triteria can be used. For example, if a merge hypothesis is generated, one possible smoothness function is

$$V = \bigcirc(G_1^*, knd, \Delta bend, support)$$

$$= \left(\frac{c_1}{knd} + \frac{c_2}{\Delta bind} + \frac{c_3}{\Delta biport}\right)$$

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nkich is maxizzen for a smooth trazsition to the next segment and lavors the straightest path hypothesis.

5.2 Compatibility and constraints

Having defined a local pairwise smoothness criterion, it is still essential to incorporate the glocal (within the junction) and global (dealing with intoke continuity) components into the interpretation. The competitivity of the image and the reconstruction in based on the event to which the interpretation agrees with the original trage. For example, given segment is and f, the pating is subject to verification that the width and intermity variations are within acceptable bornels. This information that the width and intermity of constrain the possible interpretations as well as for verification of the reconstruction is consistent with the trages. Additional compatibility measures include weiffertion that the region and all of its nontempted for, and that all of the smoothness parameters are within acceptable boundary.

Handwriting constraints can also be incorporated into the interpretation process to belo resolve ambiguity if more then one interpretation is possible. A weighing function of (i, j) can be associated with our general pairing isned, and derived from bandwriting constraints such as stroke containty, strapped octaining, or global positioning.

Both the compatibility measure and the handwriting constraints are implemented as

Both the compatibility measure and the handwriting constraints are implemented as procedural rules which effect the algorithm either locally in the case of heuristics or globally during verification.

5.3 Reconstruction

In the next section we will discuss the algorithms for interpretation. Once we have derived a feasible interpretation for the region, we recentred the occluded segment benefative as follows. If one boundary is withby, we be published to acclude durector by constructing a ribbom which is defined on one side by the visable boundary. The width of the stroke variantiform the distance between the motive points on one side of the region if to the distance between the archer points on one side of the region if to the distance between the tree should be the second to the region are constructed between the its boundary cornal sed the required between the two boundaries so that each current to be fameter of a naximal distribution to the distance of the constructed between the boundary cornal sed the cross-section and stayle at each end of the cross-section.

angle at each end of the crons-serties. Figure 6 shows some possible reconstructions. If there are no vitable boundaries or we are bridging a top in the stroke, a cribit pilet approximation is used to like the arrhor point. Uteles constray evidence entite, a tumosh transition from one stroke to the next is an appropriate assumption, and the smoothest properties of appine provide a reasonable reconstruction. The stroke then consists of the region enclosed by the two boundaries. Other features such as he medial axis and average infeatily can easily be computed by projecting the derived representation onto the original inacesty can easily be computed by projecting the derived representation onto the original inaces.

6 Region Interpretation

At the first level of Eucamianism, the type of intersection is reakly classified according to the number of segments involved, or equivalently the number of area susceinted with the code in the stroke graph. The most common intersection nodes involve 2, 3 or 4 area. If

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Figure 6: Partial reconstructions



figur I: Buic Stoke/Stoke interations: (s) High-tarruure. (b) Cotae:, (c) Merge, (d) Abulaeut, (e) Chousing.

two are are present, we hypothesize either a high-curratur point, a corner, or explore the punishility of a boundary defect. If three area are peneral, the rost likely securior indice a merger or an abeliance, and for four area, a crossing will be the princary type of interarction considered. More complex interactions which are also considered may appear as combination of these fundamental junctions; they hadred as calcaded may appear as combination of these fundamental junctions; they hadred on calcaded resuring and an incidented confect approach is to begin with a trousing hypothesis, and decompose it recursively to identify the best approach is to begin with a trousing hypothesis, and decompose it recursively to identify the best approach painting the

6.1 High-curvature points and corners

High-curvature points are the result of a single stoke segment either taving a discontinuity in currature, or having such a large curvators that a parties of the inside boundary becomes unstable (Figure 1s). The effect of this coeffgurities is the it is stoke partially overlop itself cauxing confusion in the gray level information along the inside locatedary. De order contour tends to be both while and stable and will serve as an adequate basis for determiting the stable trajectory. To reconstruct, the outer bundary is used to nector one side of the strike, and the other side is defined by the endpoint of the constructed with a width constituted with the incoming segments. The pone contour is refined according to propolitiest constructed with

A comer is a constitute discontantity in the stade trajectory and may be difficult to distinguish from a high-curvature point (Figure 75). We use the curvatures of the approaching segments and the charpeass of the other stable coalour in an alternay to distinguish between the two. If a comer interpretation can be derived, a label is attached to the region for bler analysis.

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5.2 Merges and abutments

A morpo is characterized by two segments which approach the turne trajectory, meet and continue along the same path (Figure Te and Id). The third "merged" reprent is often wider and for darter than the two approaching regments unce their puths are not likely to coincide proceedy. An abutment is characterized by one continuous stroke with the second

regment meeting it and ending.

We first attempt to identify the primary regment for the merged hypothesis, identified.

We first attempt to identify the primary regment for the regment, and is possibly as the regment which forms the largest angle with the other (we regment in inguificant, the wider. If the different is wight of the primary and approach regments is inguificant, the anches points are split, and the primary segment can be re-interpreted as a merge region or

between the approaching stroke segments is small [Figure II.] For a merge, the outer confours of the segments are windle and stable and are used to reconstruct the stroke. The inner exclours are in general unstable and eccleded as they approach the interestion. The inner eccelous is recovered by constructing cross sections of the appropriate width scornal to the outer boundary. The case where the regments merge over an extended region and The intersection of a range may occur over an extended region, especially if the angle eventually cross is discussed in the next section purt of an intersection.

If it is found that the primary segment makes a smooth transition with only one of the other segments and their widths are cimilar, an abutment is considered. Higher level mowhedge may again be required to resolve ambiguity.

6.3 Cressings and Extended Crossings

The most ecomos case of interaction is a simple exceing and is characterized by two strokes interacting at or near a 90° angle (Figure 76). When the segments are nearly outbegood, there will be no useful visible contours around the region. Unless there exist a layse discrepancy in the properties of the approaching separents, a straight stroke segment is assumed. Alterastive interpretations may be possible, and in the most general case it is medil to pass such interpretations on to higher level modules or allow reconfinan-

Two strokes which cross over an extended repon may not be detectable from only local information since it's interaction tegion may also exhibit stroke-like properties (Figure 3). This is common, for example, when the strokes meet at a low incidence angle. If two menge configurations are detected, these junctions are neighbors to the stroke graph and can be disambiguated at that point. An extended crosting may be explored in conjunction with a

8.4 Incidental Contact

at best. Since both situations occur over a keng thin region, the outer boundaries may tend to be fairly amosth. It is argueble that humans rely primarily on higher-level information about the writing for disarshignation. incidental contact occurs when two strokes meet and separate without crossing. Differentialeing between the situation of incidental contact and an extended intersection can be difficult

A simple analysis shows, however, that is order for two segments with widths a and d.



Figure 8: Cross section representation of an extended crossing





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Figure 9: Examples of incidental contact (a & b) and a complex intersection (c).

a < b, to cross at an angle $\theta \le 90^\circ$, a width of

Hanley, Flight & Zimmerman, LLC

$$\mathbf{w} = \left\{ \begin{array}{ll} \max\{\mathbf{e}_i\} & \text{if } \mathbf{a} < b \cos \delta \\ \sqrt{\left(\frac{\mathbf{a}^2 \mathbf{a} + b^2 - 2}{\epsilon_i \mathbf{a}^2}\right)^2} & \text{otherwise} \end{array} \right.$$

between the outer boundaries in the merged region must be obtained. This criterion can be used qualitatively to rule out the possibility of a croning, as in Figures 52 and b. It other cause, the boundaries may be explored for curvature discontinuities that anggest the interaction of two reparate boundaries.

6.5 Complex Interactions

to recover. The general approach described above can be extended to attempt to interpret more complete regions which contains matching teachers. For more complete regions which contains a case it seems while that the context interpretation can be derived from local information above. The only available boal information is the intensity, which may have level modules. Knowledge of the average character rise, or parish recognition results , should be considered in such studies. Similarly, when stroke interest with anthrown or non-stroke features, we preserve both the gay and filled hypothesis for higher level consideration. Complex interactions, complete stroke occlasion and interaction of segments with unknown document features fall into a class of interactions which may require non-local information ignificant differences in some nituations. This is a prime candidate for feedback from higher

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Hee-Seon Park and Seong-Whan Lee

Department of Computer Science, Changbuk National University
48 Greekhardong, Changbuk Modry Sch Konea
E-mail: swiece@thuc.changbuk ancht |
Voice: 482-431-61-2263, Fax: 482-431-279-5640

ABSTRACT

In this paper, we prepose an efficient off-line recoghilou scheme for large-set handwriten Hangil in the framework of kidden Murkow moce((JMMS) which con model stoodsatishly the frequency with narrowsy wishings that the scheme, after extracting four kinds of regional projection contracting from an input patient by using the regional projection contact markows from an input patient by using the regional projection contact markows information for HMMs are constituted based on the directled patient of contemporaling contacts during the training phase. In the recognition, place, four HMMs poststucted in the training phase are constructed to the recognition party (some statictions) of HMM parameter estimation was avoided by Imposite graph recognition, and HMM parameter estimation was avoided by Imposite graph the coupling professing time.

In order to writely the effectiveties of the proposed scheme, the most frequently used \$20 syllables by Kidtes were considered in the experiment. Experimental restricts adjusted that the proposed scheme is wery promising for the recognition of handwritten Hangel yeth contents waitsions.

i. INTRODUCTION

Recently, there are many co-going assenthes to recognize the multi-four [Anigh93, Belif9] or hundwritten strip[[leng90, Kunduled, Kunduled, Vloot92] by using this approach. For example, Kunduled all [Kunduled] have developed a handwritten Ergilish strips recognizion externe, veru to the point of using second bytet makel. These research efforts have greatly countibuted to the general understanding of the applicability of HMM to handwritten character recognition, the complexity of the parameter computation as well as the limitation of the model.

Hintarically speaking, Hangul is the Korean script which was invented abour 500 years ago. Each Korean script represents a syllable and is composed of several phoneme.

Despite many attempts to believe franching towards since 1969, it is still a very challeging problem to believe franching strang (COSA), LeeSh. The main reason for this is that a Hangel frongeridon system stould be able to classify a large and syllables which are very strains to fact and other.

This restard focuses on the use of sectionary models, to this case fills of the follow. Marko models [MAM] to recognize tardwritten fungui. HaMM have been widely used for summatic speech priograph and service funguith appear of speech strongeridan and sectionally appear of speech grant frame from the summatic strongeridan and sectionally appear of speech size on the summatic its transfer and section of speech size and strongeridan.

In process to the classification models would work on problems in changes recognition.

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Figure 10: Example cross-section representations of reconstructed strokes.

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Results and Conclusions

The intersection regions shown in the previous examples were taken from hand-printed and hand written address blacks scanned at 300 dys. Figure 10 shows the cross-scaling represen-tations of the reconstructions of some of these examples. The cross sections are added to the stocke platform along with their interpretations and the properties of the intersections.

Difficulties still remain in defining a single smoothness operator for each configuration. It is clear that higher level relations between stokes are necessary to resolve inherent ambiguisies of the local configuration. The detection of extended crossing, and incidental confacts are exampled of one compiles interpretabilists with a recommend being remoin in the system. Are the extremely an incident a more complete use of the boundary regima, a reconstruction is which the region boundaries are defined to sub-pixel accuracy, and a process which verifies the interpretation regionally.

about the nature of the case. It is clear that a real-localized representation is cusculial for such mich mich are reogration, and is one of the main difficulties for fusing such as vectorization, forms processing and tent/graphica cluctionianism. We are in the process of applying this detailed analysis approach to those interpretation to several of these productor. tigh ferd analysis tasks. Unfortwately, the deliberation of an accurate modial axis which represent sides the miling instrument trajectory or the true mid-like of a Liee segment freditionally, a thin line representation of strokes or segments has been sufficient for is not an easy task. We have provided an approach to reconstructing the original stroke segment which is based on stable properties of the electrocat and minimal assumptions

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